

# **Measurements of the Charmed Mesons Hadronic Branching Ratios at 4.03 GeV**

A Direct Measurement of  
the Absolute Branching Ratio

$$\underline{Br(D^0 \rightarrow K^-\pi^+)}$$

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## Introduction

- $Br(D^0 \rightarrow K^-\pi^+)$  and  $Br(D^+ \rightarrow K^-\pi^+\pi^+)$  are important to D physics and B physics.
  1. It's the normalization constant of BR for other D decay modes.
  2.  $b_{quark} \rightarrow (\approx 1.3)c_{quark}$
  3. The element of CKM:  $|V_{cs}|, |V_{cd}|, |V_{bd}|$
- Measurements of  $Br(D^0 \rightarrow K^-\pi^+)$  from other experiments:
  1. MarkIII (at  $\psi(3770)$ , using double tag method).
  2. ALEPH, CLEO, AUGUS etc. (at High Energy region, using decay chain  $D^{*+} \rightarrow \pi^+ D^0$ , searching for the soft pion).

There is a little difference between the result from MarkIII and that from High Energy experiments.

- BES has collected  $22 pb^{-1}$  data at 4.03 GeV. Base on this data sample, we got  $\approx 8000 D^0$  tags and  $\approx 2700 D^+$  tags .
  1. D meson may be produced via several procedures. ( $D\overline{D}^*, D^*\overline{D}^*, D\overline{D}$  , including Charged and Neutral channels).
  2. The decay of  $D^{*+}$  will cause the ‘mixing’ of  $D^0$  and  $D^+$ .
  3. Kinematical fit could not be used in analysis.
  4. Difficulty to detect the soft pions.

## Single Tags and Double Tags

Table 1. The observation possibility of single-tags and double-tags at 4.03 GeV

Modes Tags		$D\overline{D}^*$		$D^*\overline{D}^*$		$D\overline{D}$	
		$D^0\overline{D}^{*0}$	$D^-D^{*+}$	$D^{*0}\overline{D}^{*0}$	$D^{*-}D^{*+}$	$D^0\overline{D}^0$	$D^+D^-$
Single Tags	$D^0$	$2\varepsilon_i B_i$	$\varepsilon_i B_i B_0^+$	$2\varepsilon_i B_i$	$2\varepsilon_i B_i B_0^+$	$2\varepsilon_i B_i$	0
	$D^+$	0	$\varepsilon_{1i} B_i + \varepsilon_{2i} B_i (1 - B_0^+)$	0	$2\varepsilon_i B_i (1 - B_0^+)$	0	$2\varepsilon_i B_i$
Double Tags	$D^0$ vs $\overline{D}^0$	$\varepsilon_{ii} B_i B_i$ $2\varepsilon_{ij} B_i B_j$	0	$\varepsilon_{ii} B_i B_i$ $2\varepsilon_{ij} B_i B_j$	$\varepsilon_{ii} B_i B_i (B_0^+)^2$ $2\varepsilon_{ij} B_i B_j (B_0^+)^2$	$\varepsilon_{ii} B_i B_i$ $2\varepsilon_{ij} B_i B_j$	0
	$D^+$ vs $D^-$	0	$\varepsilon_{ii} B_i B_i (1 - B_0^+)$ $2\varepsilon_{ij} B_i B_j (1 - B_0^+)$	0	$\varepsilon_{ii} B_i B_i (1 - B_0^+)^2$ $2\varepsilon_{ij} B_i B_j (1 - B_0^+)^2$	0	$\varepsilon_{ii} B_i B_i$ $2\varepsilon_{ij} B_i B_j$
	$D^0$ vs $D^-$	0	$\varepsilon_{ij} B_i B_j B_0^+$	0	$2\varepsilon_{ij} B_i B_j (1 - B_0^+) B_0^+$	0	0

$$B_0^+ = Br(D^{*+} \rightarrow \pi^+ D^0)$$



## Event selection

### Single (charged) track selection

- $|\cos \theta| < 0.85$ , to insure reliable MDC measurement.
- $|V_{xy}| < 1.2\text{cm}, |V_z| < 15\text{cm}$ , tracks are required to be inside the interaction region.
- MFIT=2, -19, -9

### Particle Identification

- Pions and Kaons are required to have a relative likelihood ( $CL(type)$ ) greater than 1% for mass hypothesis, according to TOF and dE/dx information.
- More strictly cut for Kaons :  $CL(K) > CL(\pi)$ .

### Singleton D tags Selection

- D production At 4.03 GeV:
  1.  $D\overline{D}^*$  (charged and neutral)
  2.  $D^*\overline{D}^*$  (charged and neutral)
  3.  $D\overline{D}$  (charged and neutral)
- These procedures could be identified by the momentum distribution of the D-tag candidate.

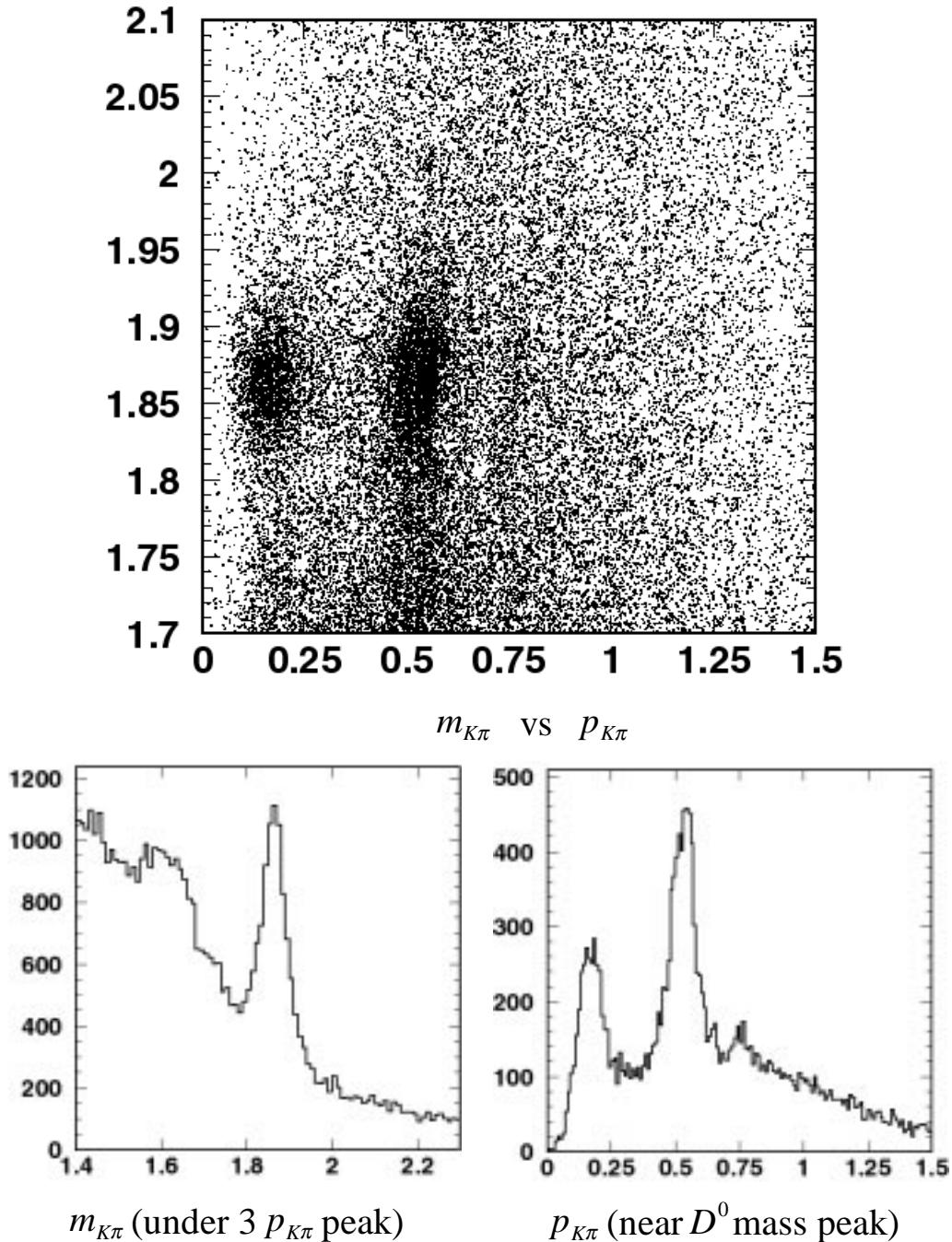


Fig1.  $m_{K\pi}$  and  $p_{K\pi}$  distribution

Fig1. shows that  $DD^*$  and  $D^*\overline{D}^*$  have large productions at 4.03 GeV. A fine momentum cut is applied to select  $D^0$  and  $D^+$  tags.

Mode	$D\bar{D}^*$	$D^*\bar{D}^*$
$D^0$	$0.42 < p < 0.64$	$0.06 < p < 0.26$
$D^+$	$0.42 < p < 0.64$	$0.04 < p < 0.24$

Table 2. Momentum cuts for  $D^0$  and  $D^+$  tags

- The production of  $D\bar{D}$  are very low, it will be discard in further analysis.

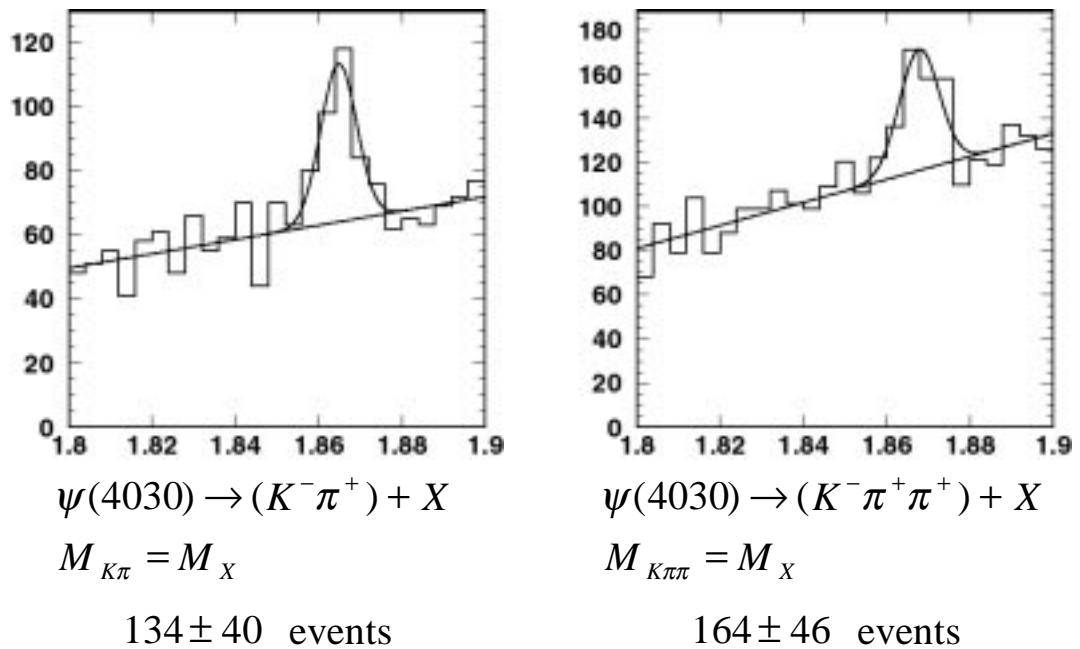


Fig2.  $M_{K\pi}$  and  $M_{K\pi\pi}$  distribution via  $D\bar{D}$  production

- Three D decay modes are selected in this analysis, they are:  $D^0 \rightarrow K^-\pi^+$ ,  $D^0 \rightarrow K^-\pi^+\pi^+\pi^-$ ,  $D^+ \rightarrow K^-\pi^+\pi^+$ . The invariant mass distributions are shown in Figure 3.

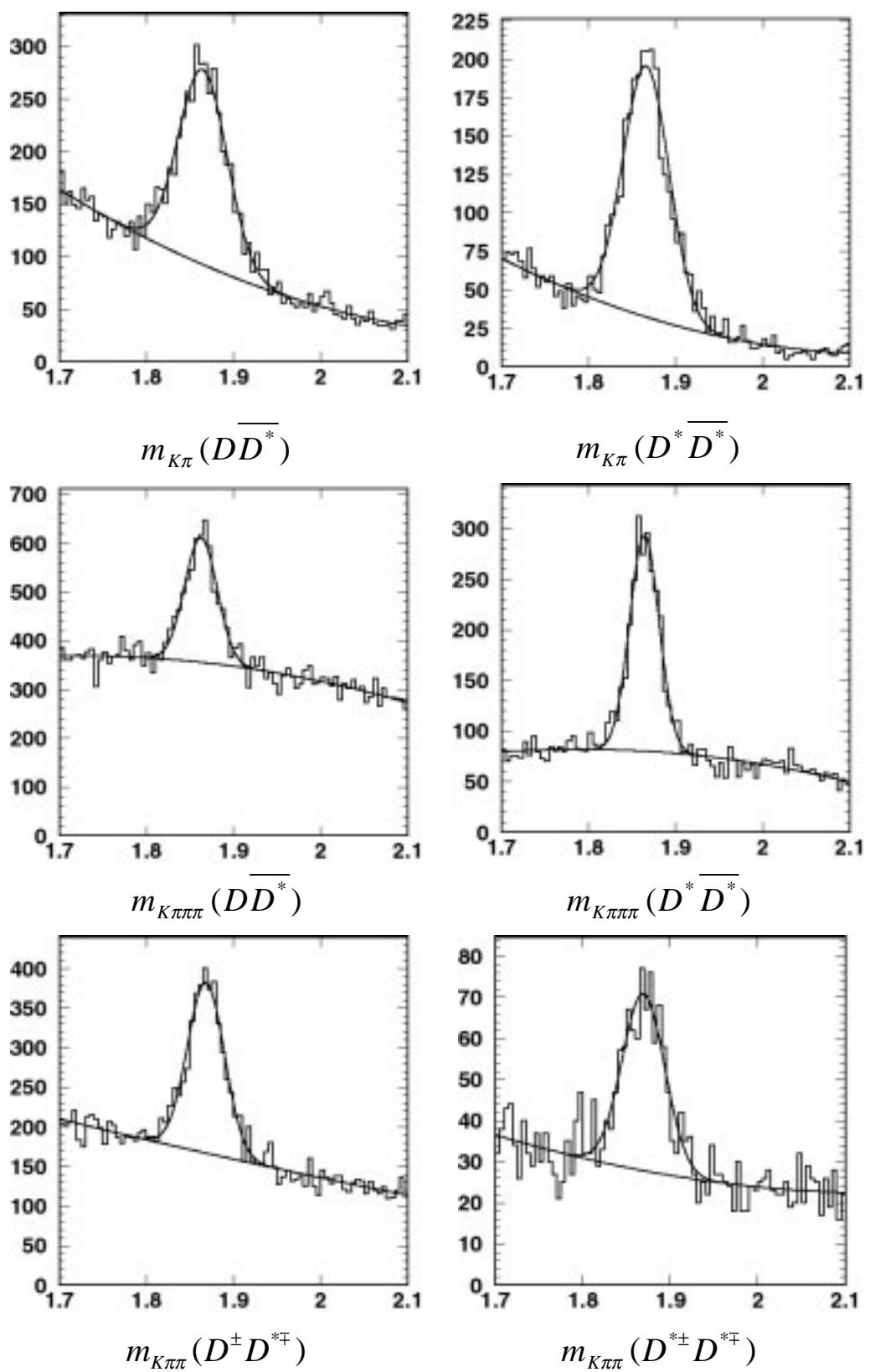
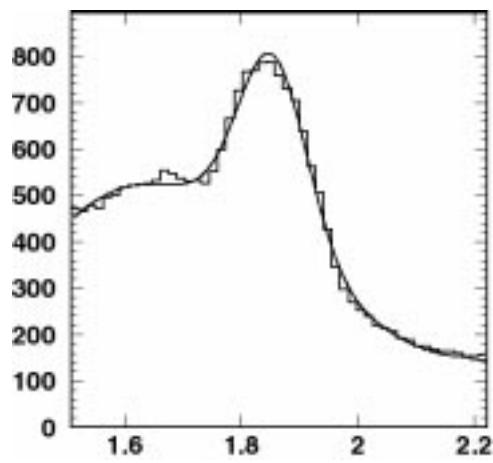
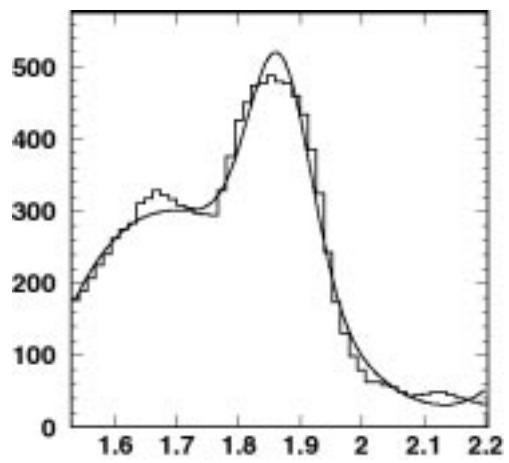
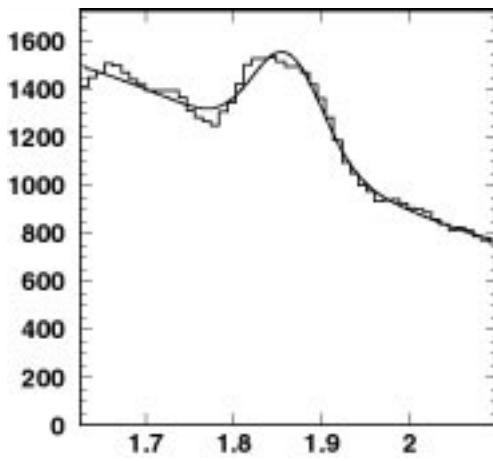
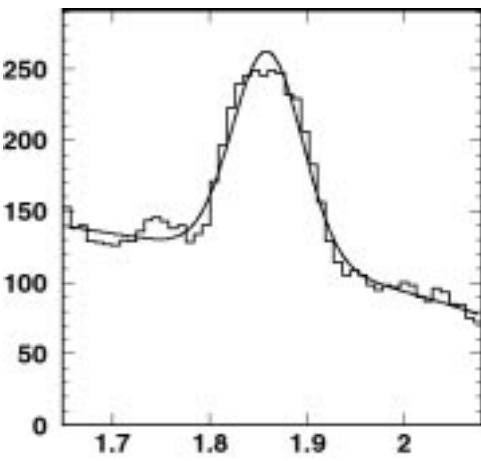
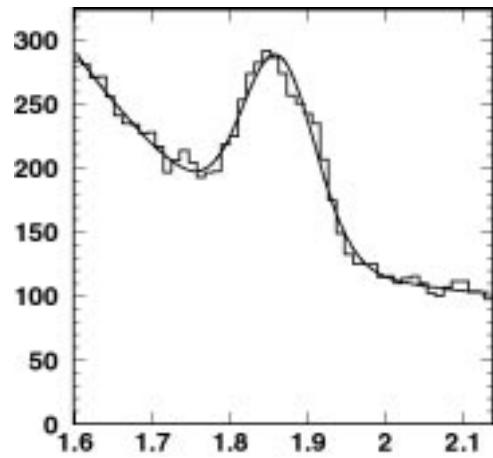
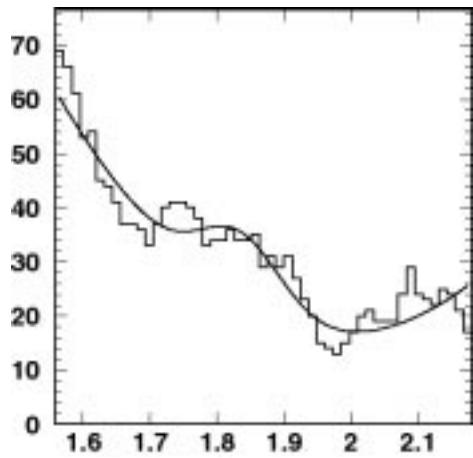


Fig 3. Invariant mass distributions for D Tag candidates

## **Double Counting Correction**

- Multi-entries:
  1. Particle misidentification
  2. Wrong combination
  3. Really double-tag events
- Keep 1 entry per event
- To evaluate the double counting ratio in signal region, a fine scan on single-tag mass plot was employed in following way:
  1. Center =  $\leftarrow M_D \rightarrow$
  2. Size =  $3\sigma_{M_D}$
  3. Step =  $0.5\sigma_{M_D}$
- Same procedure for MC data

 $K\pi(DD^*)$  $K\pi(D^*D^*)$  $K\pi\pi(DD^*)$  $K\pi\pi(D^*D^*)$  $K\pi(DD)$  $K\pi(D^*D)$ 

Double Counting Distribution

Tags		$K\pi$	$K\pi\pi\pi$	$K\pi\pi$
$D\bar{D}^*$	$M_D$	1.8647	1.8626	1.8684
	$\sigma_{M_D}$	0.0280	0.0186	0.0212
	Total Counting	$2600 \pm 101$	$2374 \pm 132$	$2290 \pm 108$
	D.C. Ratio	<u>15.4%</u>	<u>17.7%</u>	<u>6.2%</u>
	Net Counting	$2200 \pm 103$	$1954 \pm 136$	$2147 \pm 109$
$D^*\bar{D}^*$	$M_D$	1.8662	1.8641	1.8694
	$\sigma_{M_D}$	0.0265	0.0169	0.0244
	Total Counting	$2168 \pm 59$	$1799 \pm 66$	$526 \pm 52$
	D.C. Ratio	<u>14.4%</u>	<u>8.0%</u>	<u>2.1%</u>
	Net Counting	$1856 \pm 60$	$1654 \pm 67$	$515 \pm 52$



## **Double Tags Selection**

- Loosening Momentum CUT:

1. For  $D^0$  Tags:

$$0.06GeV/c < p < 0.34GeV/c$$

$$0.40GeV/c < p < 0.70GeV/c$$

2. For  $D^+$  Tags

$$0.04GeV/c < p < 0.26GeV/c$$

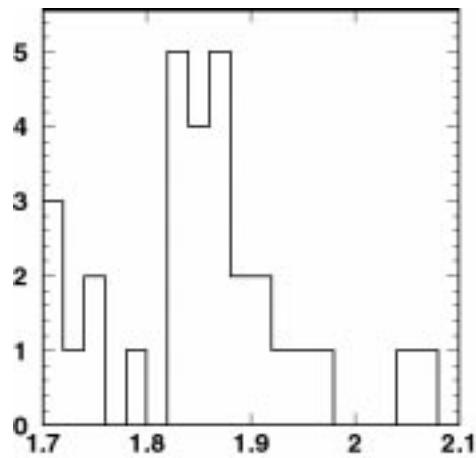
$$0.42GeV/c < p < 0.64GeV/c$$

- Tag side Mass CUT:

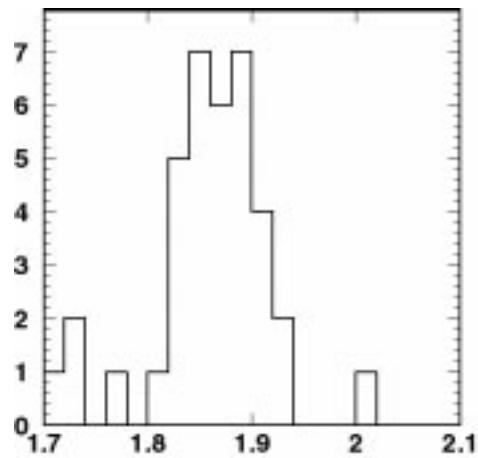
$$|M_{tag} - M_D| < 3\sigma_{M_D}$$

$M_D, \sigma_{M_D}$ , is taken from the Single Tags mass plot fit.

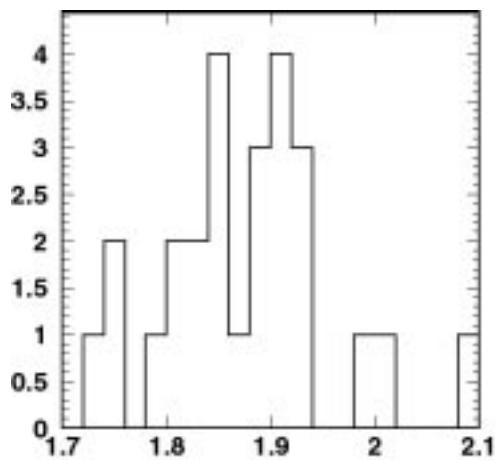
- Charm Balance is required.



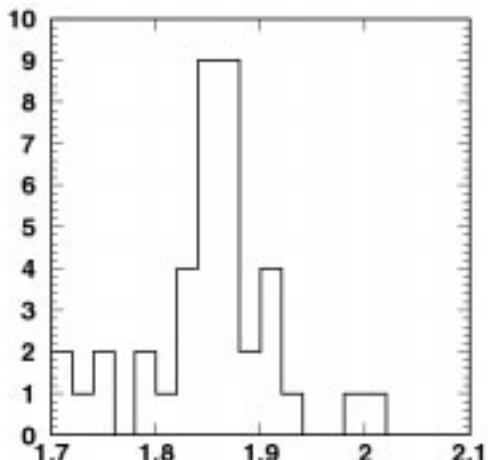
$M_{K\pi}(D\bar{D}^*)$



$M_{K\pi}(D^*\bar{D}^*)$

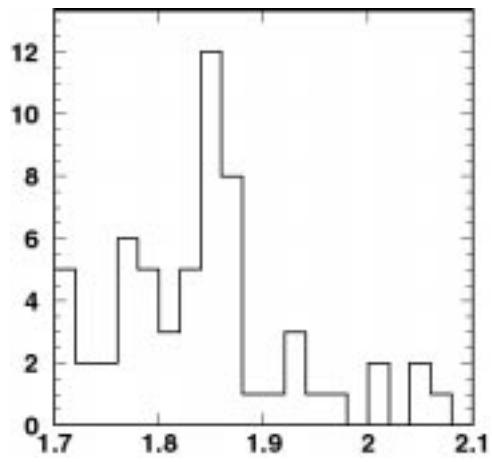


$M_{K\pi}(D\bar{D}^*)$

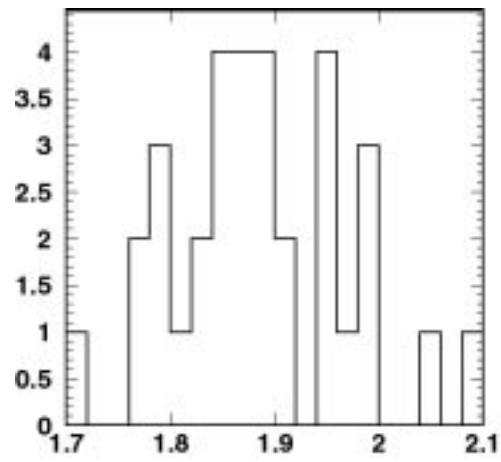


$M_{K\pi}(D^*\bar{D}^*)$

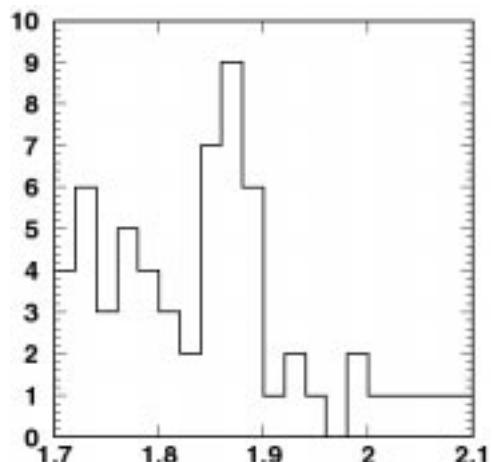
$K^- \pi^+$  vs  $K^+ \pi^-$



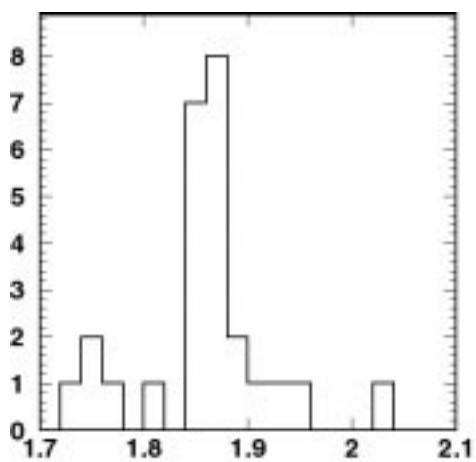
$M_{K\pi\pi\pi}(DD^*)$



$M_{K\pi\pi\pi}(D^* D^*)$

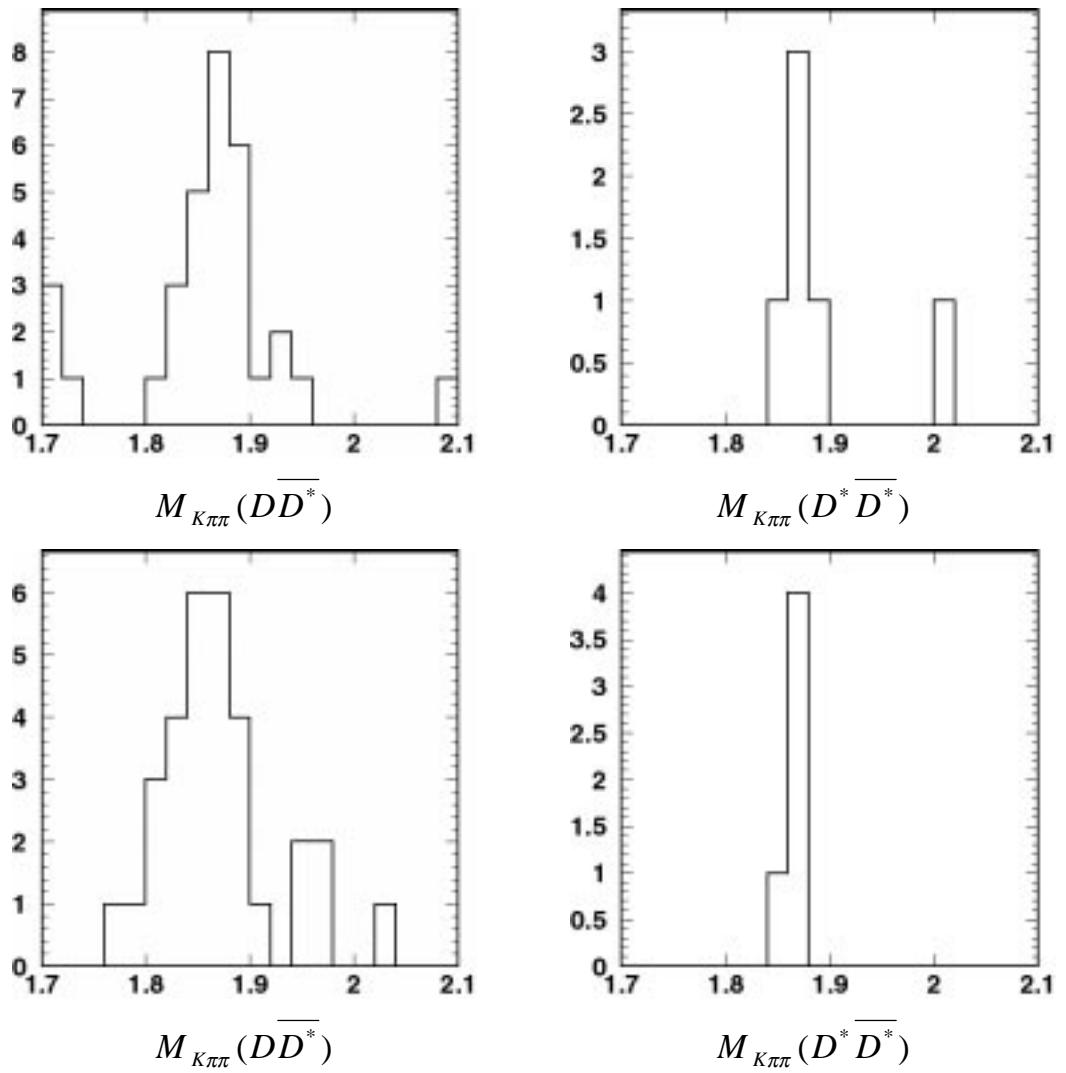


$M_{K\pi\pi\pi}(D D^*)$

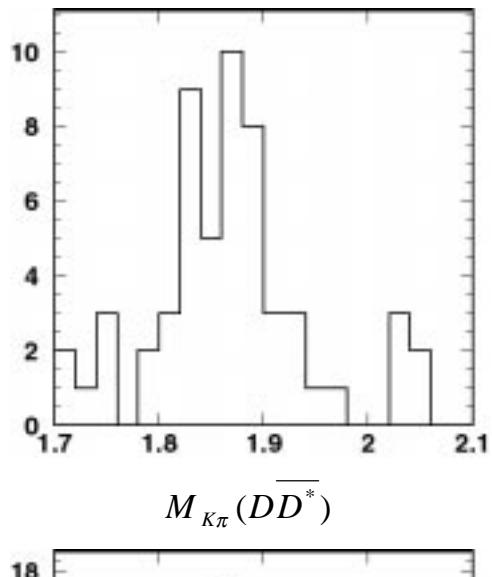
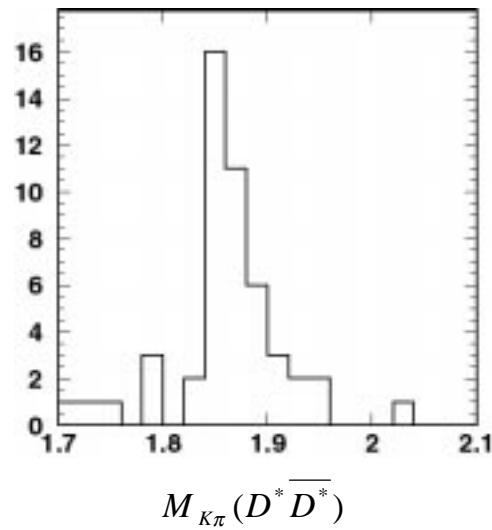
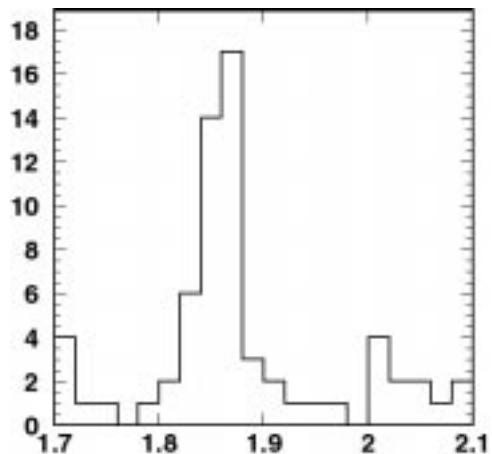
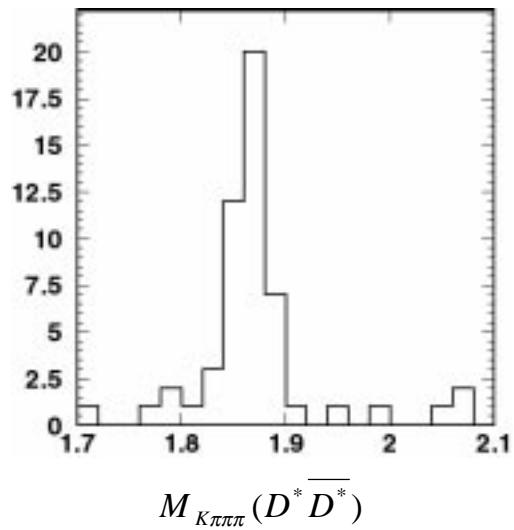


$M_{K\pi\pi\pi}(D^* D)$

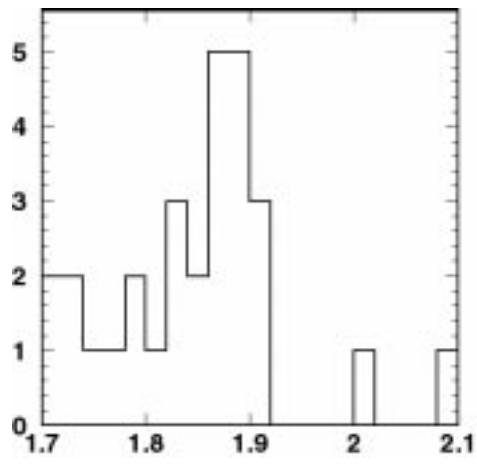
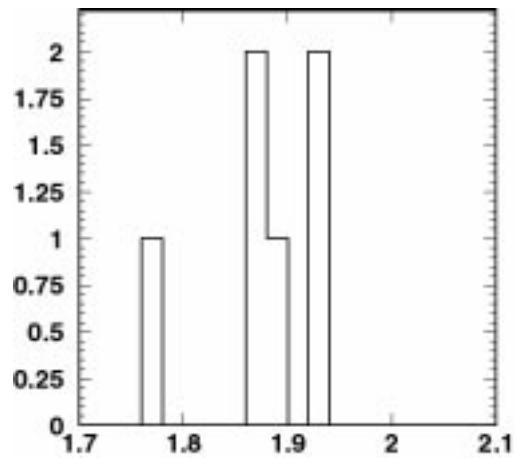
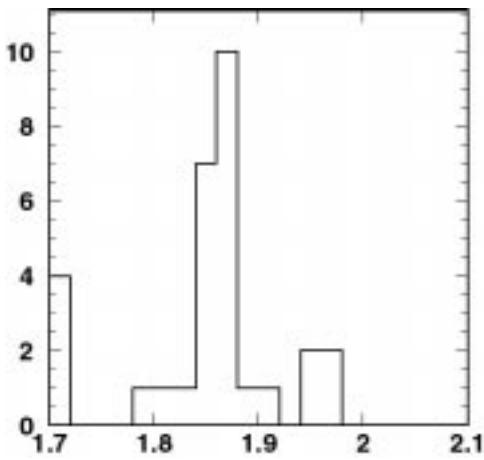
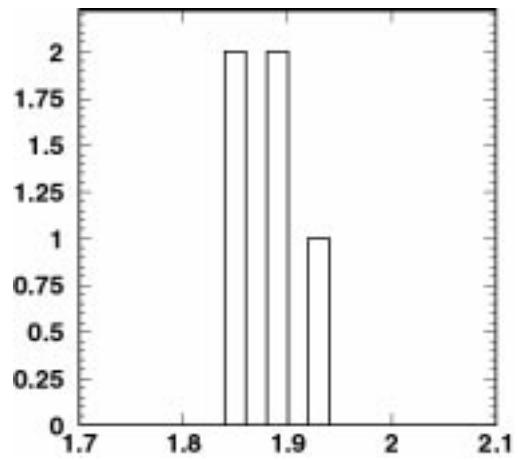
$K^- \pi^+ \pi^+ \pi^-$  vs  $K^+ \pi^- \pi^- \pi^+$

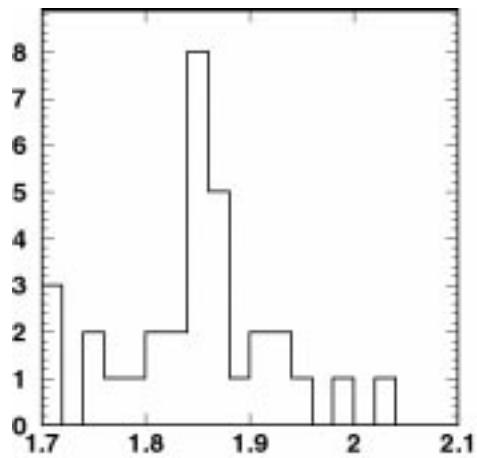
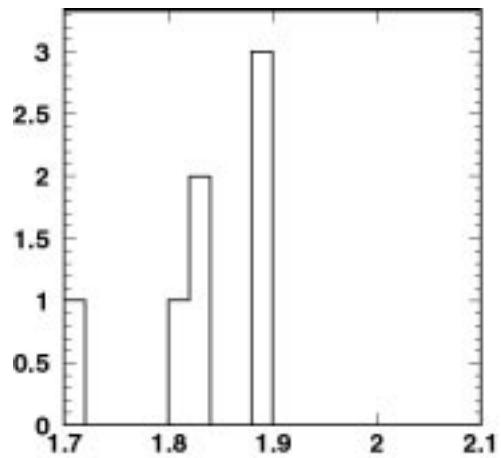
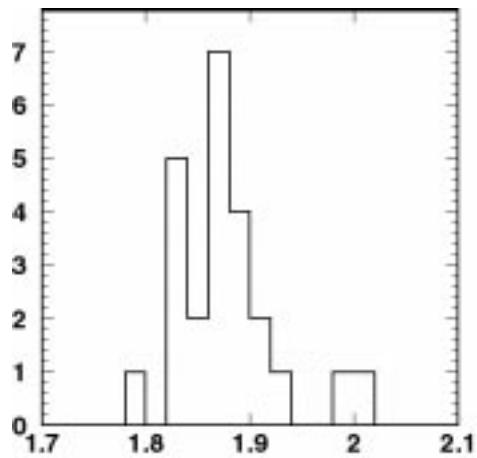
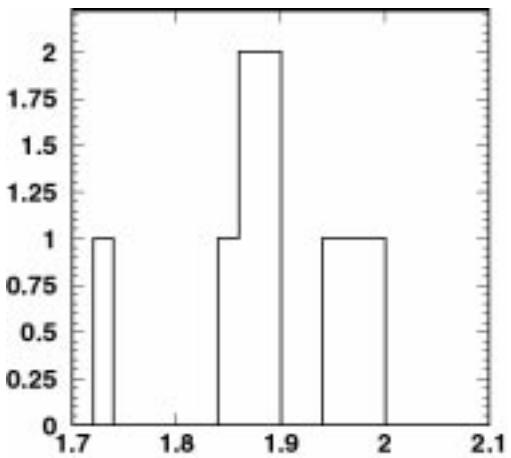


$K^- \pi^+ \pi^+$  vs  $K^+ \pi^- \pi^-$

 $M_{K\pi}(D\bar{D}^*)$  $M_{K\pi}(D^*\bar{D}^*)$  $M_{K\pi\pi\pi}(D\bar{D}^*)$  $M_{K\pi\pi\pi}(D^*\bar{D}^*)$ 

$K^- \pi^+$  vs  $K^+ \pi^- \pi^- \pi^+$

 $M_{K\pi}(DD^*)$  $M_{K\pi}(D^* D^*)$  $M_{K\pi\pi}(DD^*)$  $M_{K\pi\pi}(D^* D^*)$  $K^-\pi^+ \text{ vs } K^+\pi^-\pi^-$

 $M_{K\pi\pi\pi}(DD^*)$  $M_{K\pi\pi\pi}(D^*\bar{D}^*)$  $M_{K\pi\pi}(DD^*)$  $M_{K\pi\pi}(D^*\bar{D}^*)$  $K^-\pi^+\pi^+ \text{ vs } K^+\pi^-\pi^-\pi^+$

## **Monte Carlo efficiency**

- BES  $D\bar{D}^*$ ,  $D^*\bar{D}^*$  generator + full detector simulation at 4.03 GeV.
- Single-tags:
  1. Tag side: specified Mode via  $D$  or  $\bar{D}^*$
  2. Recoil side: cocktail (all possible modes,  $Br$  according to PDG data).
  3. Double Counting correction was made.
- Double-tags:
  1. Tag side: specified Mode via  $D$  or  $\bar{D}^*$
  2. Recoil side: specified Mode via  $D$  or  $\bar{D}^*$

## $Br(D^0 \rightarrow K^- \pi^+)$ Measurement

Data are splinted into 2 samples ( $D\overline{D}^*$ ,  $D^*\overline{D}^*$ )

1.  $D\overline{D}^*$

Let

$$N_0 = N_{D^0 \overline{D}^{*0}} = L \cdot \sigma_{D^0 \overline{D}^{*0}}$$

$$N_c = N_{D^+ D^{*-}} = L \cdot \sigma_{D^+ D^{*-}}$$

The observed Single-tags(S) and Double-tags(D) can be expressed as:

$$\begin{aligned} S_i^0 &= 2N_0 \epsilon_i B_i + N_c \epsilon_i B_i B_0^+ \\ S_i^c &= N_c \epsilon_i B_i + N_c \epsilon_i B_i (1 - B_0^+) \\ D_{ij}^{00} &= f_{ij} N_0 \epsilon_{ij} B_i B_j \\ D_{ij}^{cc} &= f_{ij} N_c \epsilon_{ij} B_i B_j (1 - B_0^+) \\ D_{ij}^{0c} &= N_c \epsilon_{ij} B_i B_j B_0^+ \end{aligned}$$

where ,

$$B_0^+ = Br(D^{*+} \rightarrow \pi^+ D^0)$$

$$f_{ij} = \begin{cases} 1 & i = j \\ 2 & i \neq j \end{cases}$$

## 2. $D^* \overline{D}^*$

Let

$$N_0 = N_{D^{*0} \overline{D}^{*0}} = L \cdot \sigma_{D^{*0} \overline{D}^{*0}}$$

$$N_c = N_{D^{*+} D^{*-}} = L \cdot \sigma_{D^{*+} D^{*-}}$$

The observed Single-tags(S) and Double-tags(D) can be expressed as:

$$\begin{aligned} S_i^0 &= 2N_0 \epsilon_i B_i + 2N_c \epsilon_i B_i B_0^+ \\ S_i^c &= 2N_c \epsilon_i B_i (1 - B_0^+) \\ D_{ij}^{00} &= f_{ij} (N_0 + N_c (B_0^+)^2) \epsilon_{ij} B_i B_j \\ D_{ij}^{cc} &= f_{ij} N_c \epsilon_{ij} B_i B_j (1 - B_0^+)^2 \\ D_{ij}^{0c} &= 2N_c \epsilon_{ij} B_i B_j B_0^+ (1 - B_0^+) \end{aligned}$$

where ,

$$B_0^+ = Br(D^{*+} \rightarrow \pi^+ D^0)$$

$$f_{ij} = \begin{cases} 1 & i = j \\ 2 & i \neq j \end{cases}$$

In final, all single-tags and double-tags are employed in a  $\chi^2$  minimization fit :

$$\chi^2 = \sum_i \frac{(S_{measure}^i - S_{pre}^i)^2}{\sigma_{S_{measure}^i}^2} + \sum_{ij} \frac{(D_{measure}^{ij} - D_{pre}^{ij})^2}{\sigma_{D_{measure}^{ij}}^2}$$

## Results

$$Br(D^0 \rightarrow K^- \pi^+) = (3.9 \pm 0.5 \pm 0.3)\%$$

$$Br(D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-) = (8.0 \pm 1.1 \pm 0.5)\%$$

$$Br(D^+ \rightarrow K^- \pi^+ \pi^+) = (9.6 \pm 3.0 \pm 0.8)\%$$

$$Br(D^{*+} \rightarrow \pi^+ D^0) = (57 \pm 10 \pm 4)\%$$

$$N_{D^0 \overline{D}^{*0}} = (5.69 \pm 1.23) \times 10^4$$

$$N_{D^{*+} D^-} = (5.23 \pm 1.55) \times 10^4$$

$$N_{D^{*0} \overline{D}^{*0}} = (4.91 \pm 0.92) \times 10^4$$

$$N_{D^{*+} D^{*-}} = (1.88 \pm 0.47) \times 10^4$$

The fit yields a  $\chi^2$  of 6.65 for 10 degrees of freedom

$$D\overline{D^*}$$

Double Tags	$K^- \pi^+$	$K^- \pi^+ \pi^+ \pi^-$	$K^- \pi^+ \pi^+$
$K^+ \pi^-$ (fit)	$14 \pm 5$ 17	$35 \pm 7$ 33	$15 \pm 6$ 16
$K^+ \pi^- \pi^- \pi^+$ (fit)		$14 \pm 6$ 19	$17 \pm 5$ 16
$K^+ \pi^- \pi^-$ (fit)			$22 \pm 5$ 22
Single Tags (fit)	$2200 \pm 103$ 2270	$1954 \pm 136$ 1754	$2147 \pm 109$ 2155

$$D^* \overline{D^*}$$

Double Tags	$K^- \pi^+$	$K^- \pi^+ \pi^+ \pi^-$	$K^- \pi^+ \pi^+$
$K^+ \pi^-$ (fit)	$25 \pm 6$ 18	$38 \pm 7$ 35	$5 \pm 3$ 6
$K^+ \pi^- \pi^- \pi^+$ (fit)		$13 \pm 5$ 18	$5 \pm 3$ 5
$K^+ \pi^- \pi^-$ (fit)			$5 \pm 3$ 4
Single Tags (fit)	$1856 \pm 60$ 1839	$1654 \pm 67$ 1684	$515 \pm 52$ 515

## Systematic Error

- Uncertainty in events selection : 3~7%
  1. Single track selection
  2. Particle identification
  3. Double counting correction
  4. Momentum CUT
  5. Sideband subtraction (Double-tags)
- Uncertainty in detection efficiency: ~5%

List of systematic errors

Term Br	Events Selection	Detection Efficiency	Total (%)
$Br(D^0 \rightarrow K^- \pi^+)$	0.2	0.2	0.3
$Br(D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-)$	0.3	0.4	0.5
$Br(D^+ \rightarrow K^- \pi^+ \pi^+)$	0.6	0.5	0.8
$Br(D^{*+} \rightarrow \pi^+ D^0)$	3.0	2.9	4.0

